

# Learning Objective

**Identify relevant and irrelevant costs and benefits in a decision.**

# Relevant Costs and Benefits

A **relevant cost** is a cost that differs between alternatives.

A **relevant benefit** is a benefit that differs between alternatives.



# Identifying Relevant Costs

An **avoidable cost** is a cost that can be eliminated, in whole or in part, by choosing one alternative over another. Avoidable costs are **relevant costs**. Unavoidable costs are **irrelevant costs**.

Two broad categories of costs are **never relevant** in any decision. They include:

- ① Sunk costs.
- ② A future cost that does not differ between the alternatives.

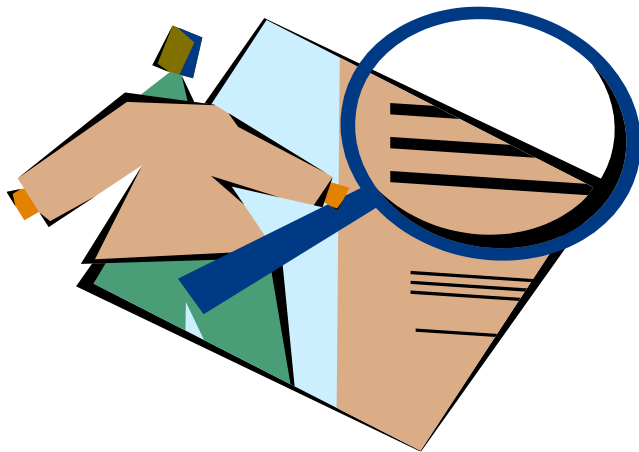
# Keys to Successful Decision-Making

1. Focus only on relevant costs (also called avoidable costs, differential costs, or incremental costs) and relevant benefits (also called differential benefits or incremental benefits).
2. Ignore everything else including sunk costs and future costs and benefits that do not differ between the alternatives.





# Different Costs for Different Purposes



Costs that are relevant in one decision situation **may not be relevant** in another context.

Thus, in each decision situation, the manager must examine the data at hand and isolate the relevant costs.

# Identifying Relevant Costs

Cynthia, a Boston student, is considering visiting her friend in New York. She can drive or take the train. By car, it is 230 miles to her friend's apartment. She is trying to decide which alternative is less expensive and has gathered the following information.

Automobile Costs (based on 10,000 miles driven per year)		
	Annual Cost of Fixed Items	Cost per Mile
1 Annual straight-line depreciation on car	\$ 2,800	\$ 0.280
2 Cost of gasoline		0.100
3 Annual cost of auto insurance and license	1,380	0.138
4 Maintenance and repairs		0.065
5 Parking fees at school	360	0.036
6 Total average cost		\$ 0.619

\$45 per month × 8 months

\$2.70 per gallon ÷ 27 MPG

\$24,000 cost – \$10,000 salvage value ÷ 5 years

# Identifying Relevant Costs

<b>Automobile Costs (based on 10,000 miles driven per year)</b>		
	<u>Annual Cost of Fixed Items</u>	<u>Cost per Mile</u>
1 Annual straight-line depreciation on car	\$ 2,800	\$ 0.280
2 Cost of gasoline		0.100
3 Annual cost of auto insurance and license	1,380	0.138
4 Maintenance and repairs		0.065
5 Parking fees at school	360	0.036
6 Total average cost		<u>\$ 0.619</u>

<b>Additional Information</b>		
7 Reduction in resale value of car per mile of wear	\$	0.026
8 Round-trip train fare	\$	104
9 Benefits of relaxing on train trip		????
10 Cost of putting dog in kennel while gone	\$	40
11 Benefit of having car in New York		????
12 Hassle of parking car in New York		????
13 Per day cost of parking car in New York	\$	25

# Identifying Relevant Costs

Which costs and benefits are relevant in Cynthia's decision?

The cost of the car is a sunk cost and is **not relevant** to the current decision.

The annual cost of insurance is **not relevant**. It will remain the same if she drives or takes the train.

However, the cost of gasoline is clearly **relevant** if she decides to drive. If she takes the train, the cost would not be incurred, so it varies depending on the decision.

# Identifying Relevant Costs

Which costs and benefits are relevant in Cynthia's decision?

The cost of maintenance and repairs is **relevant**. In the long-run these costs depend upon miles driven.

The monthly school parking fee is **not relevant** because it must be paid if Cynthia drives or takes the train.

At this point, we can see that some of the average cost of \$0.619 per mile are relevant and others are not.

# Identifying Relevant Costs

Which costs and benefits are relevant in Cynthia's decision?

The decline in resale value due to additional miles is a **relevant** cost.

The round-trip train fare is clearly **relevant**. If she drives the cost can be avoided.

Relaxing on the train is **relevant** even though it is difficult to assign a dollar value to the benefit.

The kennel cost is **not relevant** because Cynthia will incur the cost if she drives or takes the train.

# Identifying Relevant Costs

Which costs and benefits are relevant in Cynthia's decision?

The cost of parking in New York is **relevant** because it can be avoided if she takes the train.

The benefits of having a car in New York and the problems of finding a parking space are both **relevant** but are difficult to assign a dollar amount.

# Identifying Relevant Costs

**From a financial standpoint, Cynthia would be better off taking the train to visit her friend. Some of the non-financial factors may influence her final decision.**

<b>Relevant Financial Cost of Driving</b>	
Gasoline (460 @ \$0.100 per mile)	\$ 46.00
Maintenance (460 @ \$0.065 per mile)	29.90
Reduction in resale (460 @ \$0.026 per mile)	11.96
Parking in New York (2 days @ \$25 per day)	50.00
<b>Total</b>	<b><u>\$ 137.86</u></b>

<b>Relevant Financial Cost of Taking the Train</b>	
Round-trip ticket	<b><u>\$ 104.00</u></b>



# Total and Differential Cost Approaches

The management of a company is considering a new labor saving machine that rents for \$3,000 per year. Data about the company's annual sales and costs with and without the new machine are:

	Current Situation	Situation With New Machine	Differential Costs and Benefits
Sales (5,000 units @ \$40 per unit)	\$ 200,000	\$ 200,000	-
Less variable expenses:			
Direct materials (5,000 units @ \$14 per unit)	70,000	70,000	-
Direct labor (5,000 units @ \$8 and \$5 per unit)	40,000	25,000	15,000
Variable overhead (5,000 units @ \$2 per unit)	10,000	10,000	-
Total variable expenses	120,000	105,000	-
Contribution margin	80,000	95,000	15,000
Less fixed expense:			
Other	62,000	62,000	-
Rent on new machine	-	3,000	(3,000)
Total fixed expenses	62,000	65,000	(3,000)
Net operating income	\$ 18,000	\$ 30,000	12,000

# Total and Differential Cost Approaches

As you can see, the only costs that differ between the alternatives are the direct labor costs savings and the increase in fixed rental costs.

	Current Situation	Situation With New Machine	Differential Costs and Benefits
Sales (5,000 units @ \$40 per unit)	\$ 200,000	\$ 200,000	-
Less variable expenses:			
Direct materials			-
Direct labor			15,000
Variable overhead			-
Total variable expenses			-
Contribution margin			15,000
Less fixed expenses:			
Other			-
Rent on new machine			(3,000)
Total fixed expenses			(3,000)
Net operating income			12,000

<b>Net Advantage to Renting the New Machine</b>	
Decrease in direct labor costs (5,000 units @ \$3 per unit)	\$ 15,000
Increase in fixed rental expenses	(3,000)
Net annual cost saving from renting the new machine	<u>\$ 12,000</u>

**We can efficiently analyze the decision by looking at the different costs and revenues and arrive at the same solution.**

# Total and Differential Cost Approaches

**Using the differential approach is desirable for two reasons:**

- 1. Only rarely will enough information be available to prepare detailed income statements for both alternatives.**
- 2. Mingling irrelevant costs with relevant costs may cause confusion and distract attention away from the information that is really critical.**

# Learning Objective

**Prepare an analysis showing whether a product line or other business segment should be added or dropped.**

# Adding/Dropping Segments

**One of the most important decisions managers make is whether to add or drop a business segment.**

**Ultimately, a decision to drop an old segment or add a new one is going to hinge primarily on the impact the decision will have on net operating income.**



**To assess this impact, it is necessary to carefully analyze the costs.**

# Adding/Dropping Segments



**Due to the declining popularity of digital watches, Lovell Company's digital watch line has not reported a profit for several years. Lovell is considering discontinuing this product line.**

# A Contribution Margin Approach



## ***DECISION RULE***

**Lovell should drop the digital watch segment only if its profit would increase.**

**Lovell will compare the contribution margin that would be lost to the costs that would be avoided if the line was to be dropped.**

# Adding/Dropping Segments



## Segment Income Statement Digital Watches

<b>Sales</b>		<b>\$ 500,000</b>
<b>Less: variable expenses</b>		
Variable manufacturing costs	<b>\$ 120,000</b>	
Variable shipping costs	<b>5,000</b>	
Commissions	<b>75,000</b>	<b>200,000</b>
		<hr/>
<b>Contribution margin</b>		<b>\$ 300,000</b>
<b>Less: fixed expenses</b>		
General factory overhead	<b>\$ 60,000</b>	
Salary of line manager	<b>90,000</b>	
Depreciation of equipment	<b>50,000</b>	
Advertising - direct	<b>100,000</b>	
Rent - factory space	<b>70,000</b>	
General admin. expenses	<b>30,000</b>	<b>400,000</b>
		<hr/>
<b>Net operating loss</b>		<b>\$ (100,000)</b>



# Adding/Dropping Segments



## Segment Income Statement Digital Watches

Sales \$ 500,000

**An investigation has revealed that the fixed general factory overhead and fixed general administrative expenses will not be affected by dropping the digital watch line. The fixed general factory overhead and general administrative expenses assigned to this product would be reallocated to other product lines.**

Advertising - direct	100,000	
Rent - factory space	70,000	
General admin. expenses	30,000	400,000
Net operating loss		<u>\$ (100,000)</u>

# Adding/Dropping Segments



## Segment Income Statement Digital Watches

<b>Sales</b>		<b>\$ 500,000</b>
<p>The equipment used to manufacture digital watches has no resale value or alternative use.</p>		
		<u>200,000</u>
<b>Contribution margin</b>		<b>\$ 300,000</b>
<b>Less: fixed expenses</b>		
General factory overhead	\$ 60,000	
Salary of line manager	20,000	
Depreciation of equipment	10,000	
Advertising - direct	10,000	
Rent - factory space	70,000	
General admin. expenses	30,000	
	<u>200,000</u>	
<b>Net operating loss</b>		<b>\$ (100,000)</b>

**Should Lovell retain or drop the digital watch segment?**

# A Contribution Margin Approach



## Contribution Margin Solution

<b>Contribution margin lost if digital watches are dropped</b>		<b>\$ (300,000)</b>
<b>Less fixed costs that can be avoided</b>		
Salary of the line manager	\$ 90,000	
Advertising - direct	100,000	
Rent - factory space	70,000	260,000
<b>Net disadvantage</b>		<b>\$ (40,000)</b>



# Comparative Income Approach



**The Lovell solution can also be obtained by preparing comparative income statements showing results with and without the digital watch segment.**

**Let's look at this second approach.**



## Comparative Income Approach Solution

	Keep Digital Watches	Drop Digital Watches	Difference
<b>Sales</b>	<u>\$ 500,000</u>	<u>\$ -</u>	<u>\$ (500,000)</u>
<b>Less variable expenses:</b>			
Manufacturing expenses	120,000	-	120,000
Shipping	5,000	-	5,000
Commissions	<u>75,000</u>	-	<u>75,000</u>
<b>Total variable expenses</b>	<u>200,000</u>	<u>-</u>	<u>200,000</u>
<b>Contribution margin</b>	<u>300,000</u>	<u>-</u>	<u>(300,000)</u>
<b>Less fixed expenses:</b>			
General factory overhead	60,000		
Salary of line manager	90,000		
Depreciation	50,000		
Advertising - direct	100,000		
Rent - factory space	70,000		
General admin. expenses	<u>30,000</u>		
<b>Total fixed expenses</b>	<u>400,000</u>		
<b>Net operating loss</b>	<u><u>\$ (100,000)</u></u>		

If the digital watch line is dropped, the company loses \$300,000 in contribution margin.



## Comparative Income Approach Solution

	Keep Digital Watches	Drop Digital Watches	Difference
<b>Sales</b>	<u>\$ 500,000</u>	<u>\$ -</u>	<u>\$ (500,000)</u>
<b>Less variable expenses:</b>			
<b>Manufacturing expenses</b>	120,000	-	120,000
<b>Shipping</b>	5,000	-	5,000
<b>Commissions</b>	<u>75,000</u>	-	<u>75,000</u>
<b>Total variable expenses</b>	<u>200,000</u>	<u>-</u>	<u>200,000</u>
<b>Contribution margin</b>	<u>300,000</u>	<u>-</u>	<u>(300,000)</u>
<b>Less fixed expenses:</b>			
<b>General factory overhead</b>	60,000	60,000	-
<b>Salary of line manager</b>	90,000		
<b>Depreciation</b>			
<b>Advertising - direct</b>			
<b>Rent - factory space</b>			
<b>General admin. expenses</b>			
<b>Total fixed expenses</b>			
<b>Net operating loss</b>			

On the other hand, the general factory overhead would be the same under both alternatives, so it is irrelevant.



## Comparative Income Approach Solution

	Keep Digital Watches	Drop Digital Watches	Difference
<b>Sales</b>	\$ 500,000	\$ -	\$ (500,000)
<b>Less variable expenses:</b>			
Manufacturing expenses			120,000
Shipping			5,000
Commissions			75,000
<b>Total variable expenses</b>	<u>200,000</u>		<u>200,000</u>
<b>Contribution margin</b>	<u>300,000</u>	<u>-</u>	<u>(300,000)</u>
<b>Less fixed expenses:</b>			
General factory overhead	60,000	60,000	-
Salary of line manager	90,000	-	90,000
Depreciation	50,000		
Advertising - direct	100,000		
Rent - factory space	70,000		
General admin. expenses	30,000		
<b>Total fixed expenses</b>	<u>400,000</u>		
<b>Net operating loss</b>	<u>\$ (100,000)</u>		

The salary of the product line manager would disappear, so it is relevant to the decision.



## Comparative Income Approach Solution

	Keep Digital Watches	Drop Digital Watches	Difference
Sales	\$ 500,000	\$ 500,000	\$ (500,000)
Less variable expenses:			
Direct materials	100,000	100,000	-
Direct labor	100,000	100,000	-
Manufacturing overhead	100,000	100,000	-
Selling expenses	50,000	50,000	-
Administrative expenses	50,000	50,000	-
Contribution margin	<u>300,000</u>	<u>-</u>	<u>(300,000)</u>
Less fixed expenses:			
General factory overhead	60,000	60,000	-
Salary of line manager	90,000	-	90,000
Depreciation	50,000	50,000	-
Advertising - direct	100,000	-	100,000
Rent - factory space	70,000	-	70,000
General admin. expenses	30,000	-	30,000
Total fixed expenses	<u>400,000</u>	<u>110,000</u>	<u>(290,000)</u>
Net operating loss	<u>\$ (100,000)</u>	<u>\$ (110,000)</u>	<u>\$ 10,000</u>

The depreciation is a sunk cost. Also, remember that the equipment has no resale value or alternative use, so the equipment and the depreciation expense associated with it are irrelevant to the decision.





## Comparative Income Approach Solution

	Keep Digital Watches	Drop Digital Watches	Difference
<b>Sales</b>	<u>\$ 500,000</u>	<u>\$ -</u>	<u>\$ (500,000)</u>
<b>Less variable expenses:</b>			
Manufacturing expense	100,000	-	100,000
Shipping	5,000	-	5,000
Commissions	20,000	-	20,000
<b>Total variable expenses</b>	<u>125,000</u>	<u>-</u>	<u>125,000</u>
<b>Contribution margin</b>	<u>375,000</u>	<u>0</u>	<u>(375,000)</u>
<b>Less fixed expenses:</b>			
General factory overhead	-	-	-
Salary of line manager	50,000	-	50,000
Depreciation	50,000	50,000	-
Advertising - direct	100,000	-	100,000
Rent - factory space	70,000	-	70,000
General admin. expenses	30,000	30,000	-
<b>Total fixed expenses</b>	<u>400,000</u>	<u>140,000</u>	<u>260,000</u>
<b>Net operating loss</b>	<u><u>\$ (100,000)</u></u>	<u><u>\$ (140,000)</u></u>	<u><u>\$ (40,000)</u></u>

The complete comparative income statements reveal that Lovell would earn \$40,000 of additional profit by retaining the digital watch line.

# Beware of Allocated Fixed Costs



Why should we keep the  
digital watch segment  
when it's showing a  
**\$100,000 loss?**



# Beware of Allocated Fixed Costs



The answer lies in the way we allocate **common fixed costs** to our products.



# Beware of Allocated Fixed Costs



Including **unavoidable common fixed costs** makes the product line appear to be unprofitable.

Our allocations can make a segment look **less profitable** than it really is.

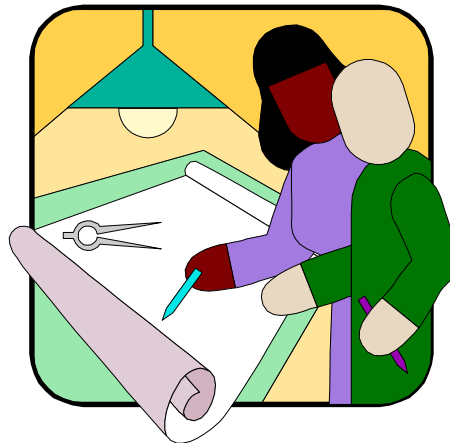


# Learning Objective 10-3

**Prepare a make or buy analysis.**

# The Make or Buy Decision

When a company is involved in more than one activity in the entire value chain, it is vertically integrated. A decision to carry out one of the activities in the value chain internally, rather than to buy externally from a supplier is called a “**make or buy**” decision.



# The Make or Buy Decision: An Example

Essex Company manufactures part 4A that is used in one of its products. The unit product cost of this part is:

<b>Direct materials</b>	<b>\$ 9</b>
<b>Direct labor</b>	<b>5</b>
<b>Variable overhead</b>	<b>1</b>
<b>Depreciation of special equip.</b>	<b>3</b>
<b>Supervisor's salary</b>	<b>2</b>
<b>General factory overhead</b>	<b>10</b>
<b>Unit product cost</b>	<b><u>\$ 30</u></b>

# The Make or Buy Decision

- The special equipment used to manufacture part 4A has no resale value.
- The total amount of general factory overhead, which is allocated on the basis of direct labor hours, would be unaffected by this decision.
- The \$30 unit product cost is based on 20,000 parts produced each year.
- An outside supplier has offered to provide the 20,000 parts at a cost of \$25 per part.

**Should Essex make or buy part 4A?**



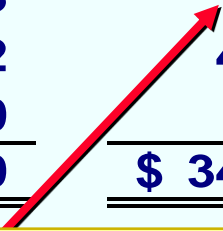
# The Make or Buy Decision

	Cost Per Unit	Cost of 20,000 Units	
		Make	Buy
Outside purchase price	<u>\$ 25</u>		\$ 500,000
Direct materials (20,000 units)	\$ 9	180,000	
Direct labor	5	100,000	
Variable overhead	1	20,000	
Depreciation of equip.	3	-	
Supervisor's salary	2	40,000	
General factory overhead	10	-	
Total cost	<u>\$ 30</u>	<u>\$ 340,000</u>	<u>\$ 500,000</u>

The **avoidable costs** associated with making part 4A include direct materials, direct labor, variable overhead, and the supervisor's salary.

# The Make or Buy Decision

	Cost Per Unit	Cost of 20,000 Units	
		Make	Buy
Outside purchase price	<u>\$ 25</u>		<u>\$ 500,000</u>
Direct materials (20,000 units)	\$ 9	180,000	
Direct labor	5	100,000	
Variable overhead	1	20,000	
Depreciation of equip.	3	-	
Supervisor's salary	2	40,000	
General factory overhead	10	-	
Total cost	<u>\$ 30</u>	<u>\$ 340,000</u>	<u>\$ 500,000</u>



The depreciation of the special equipment represents a **sunk cost**. The equipment has no resale value, thus its cost and associated depreciation are irrelevant to the decision.

# The Make or Buy Decision

	Cost Per Unit	Cost of 20,000 Units	
		Make	Buy
<b>Outside purchase price</b>	<b>\$ 25</b>		<b>\$ 500,000</b>
Direct materials (20,000 units)	\$ 9	180,000	
Direct labor	5	100,000	
Variable overhead	1	20,000	
Depreciation of equip.	3	-	
Supervisor's salary	2	40,000	
General factory overhead	10	-	
<b>Total cost</b>	<b>\$ 30</b>	<b>\$ 340,000</b>	<b>\$ 500,000</b>

Not avoidable; irrelevant. If the product is dropped, it will be reallocated to other products.

# The Make or Buy Decision

	Cost Per Unit	Cost of 20,000 Units	
		Make	Buy
<b>Outside purchase price</b>	<b>\$ 25</b>		<b>\$ 500,000</b>
Direct materials (20,000 units)	\$ 9	180,000	
Direct labor	5	100,000	
Variable overhead	1	20,000	
Depreciation of equip.	3	-	
Supervisor's salary	2	40,000	
General factory overhead	10	-	
<b>Total cost</b>	<b>\$ 30</b>	<b>\$ 340,000</b>	<b>\$ 500,000</b>

**Should we make or buy part 4A?**

Given that the total avoidable costs are less than the cost of buying the part, **Essex should continue to make the part.**

# Opportunity Cost

An **opportunity cost** is the benefit that is foregone as a result of pursuing some course of action.

Opportunity costs are not actual cash outlays and are not recorded in the formal accounts of an organization.

If Essex had an alternative use for the capacity that it used to make part 4A, there would have been an opportunity cost to factor into the analysis.



# Learning Objective 10-4

**Prepare an analysis showing whether a special order should be accepted.**

# Key Terms and Concepts

A **special order** is a one-time order that is not considered part of the company's normal ongoing business.

When analyzing a special order, only the **incremental costs and benefits** are relevant.

Since the existing fixed manufacturing overhead costs would not be affected by the order, they are not relevant.



# Special Orders

- **Jet Inc. makes a single product whose normal selling price is \$20 per unit.**
- **A foreign distributor offers to purchase 3,000 units for \$10 per unit.**
- **This is a one-time order that would not affect the company's regular business.**
- **Annual capacity is 10,000 units, but Jet Inc. is currently producing and selling only 5,000 units.**

**Should Jet accept the offer?**



# Special Orders

<b>Jet Inc.</b>		
<b>Contribution Income Statement</b>		
<b>Revenue (5,000 × \$20)</b>		<b>\$ 100,000</b>
<b>Variable costs:</b>		
<b>Direct materials</b>	<b>\$ 20,000</b>	
<b>Direct labor</b>	<b>5,000</b>	
<b>Manufacturing overhead</b>	<b>10,000</b>	
<b>Marketing costs</b>	<b>5,000</b>	
<b>Total variable costs</b>	<b>40,000</b>	
<b>Contribution margin</b>		<b>60,000</b>
<b>Fixed costs:</b>		
<b>Manufacturing overhead</b>	<b>\$ 28,000</b>	
<b>Marketing costs</b>	<b>20,000</b>	
<b>Total fixed costs</b>		<b>48,000</b>
<b>Net operating income</b>		<b>\$ 12,000</b>

**\$8 variable cost**

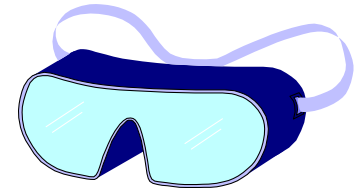
# Special Orders

If Jet accepts the special order, the incremental revenue will exceed the incremental costs. In other words, net operating income will increase by \$6,000. This suggests that Jet should accept the order.

Increase in revenue (3,000 × \$10)	<b>\$30,000</b>
Increase in costs (3,000 × \$8 variable cost)	<b>24,000</b>
Increase in net income	<b><u>\$ 6,000</u></b>

**Note:** This answer assumes that the fixed costs are **unavoidable** and that variable marketing costs must be incurred on the special order.

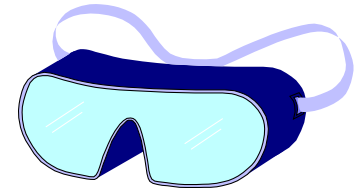
## Quick Check ✓



Northern Optical ordinarily sells the X-lens for \$50. The variable production cost is \$10, the fixed production cost is \$18 per unit, and the variable selling cost is \$1. A customer has requested a special order for 10,000 units of the X-lens to be imprinted with the customer's logo. This special order would not involve any selling costs, but Northern Optical would have to purchase an imprinting machine for \$50,000.

(see the next page)

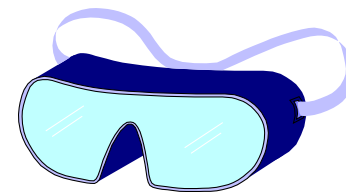
# Quick Check ✓



What is the rock bottom minimum price below which Northern Optical should not go in its negotiations with the customer? In other words, below what price would Northern Optical actually be losing money on the sale? There is ample idle capacity to fulfill the order and the imprinting machine has no further use after this order.

- a. \$50
- b. \$10
- c. \$15
- d. \$29

# Quick Check ✓



What is the rock bottom minimum price below which Northern Optical should not go in its negotiations with the customer? In other words, below what price would Northern Optical actually be losing money on the sale? There is ample idle capacity to fulfill the order and the imprinting machine has no further use for this machine.

- a. \$50
- b. \$10
- c. \$15**
- d. \$29

<b>Variable production cost</b>	<b>\$100,000</b>
<b>Additional fixed cost</b>	<b>+ 50,000</b>
<b>Total relevant cost</b>	<b><u>\$150,000</u></b>
<b>Number of units</b>	<b>10,000</b>
<b>Average cost per unit=</b>	<b>\$15</b>

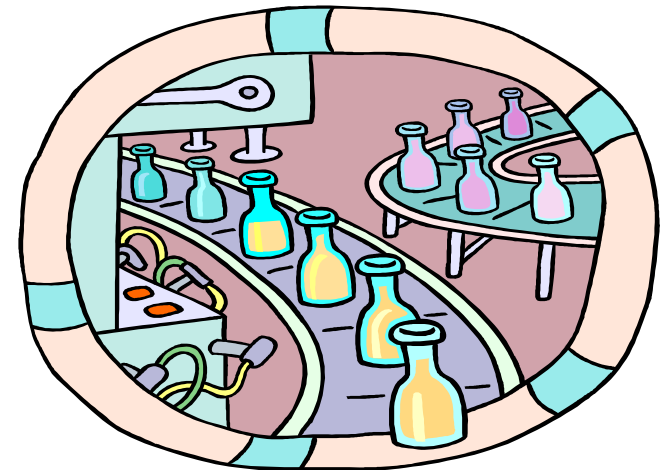
# Learning Objective 10-5

**Determine the most profitable use of a constrained resource.**

# Key Terms and Concepts

When a limited resource of some type restricts the company's ability to satisfy demand, the company is said to have a **constraint**.

The machine or process that is limiting overall output is called the **bottleneck** – it is the constraint.



# Utilization of a Constrained Resource

- **Fixed costs are usually unaffected in these situations, so the product mix that maximizes the company's total contribution margin should ordinarily be selected.**
- **A company should not necessarily promote those products that have the highest unit contribution margins.**
- **Rather, total contribution margin will be maximized by promoting those products or accepting those orders that provide the highest contribution margin in relation to the constraining resource.**



# Utilization of a Constrained Resource: An Example

Ensign Company produces two products and selected data are shown below:

	<b>Product</b>	
	<b>1</b>	<b>2</b>
<b>Selling price per unit</b>	<b>\$ 60</b>	<b>\$ 50</b>
<b>Less variable expenses per unit</b>	<b>36</b>	<b>35</b>
<b>Contribution margin per unit</b>	<b>\$ 24</b>	<b>\$ 15</b>
<b>Current demand per week (units)</b>	<b>2,000</b>	<b>2,200</b>
<b>Contribution margin ratio</b>	<b>40%</b>	<b>30%</b>
<b>Processing time required on machine A1 per unit</b>	<b>1.00 min.</b>	<b>0.50 min.</b>

# Utilization of a Constrained Resource: An Example

- **Machine A1 is the constrained resource and is being used at 100% of its capacity.**
- **There is excess capacity on all other machines.**
- **Machine A1 has a capacity of 2,400 minutes per week.**

**Should Ensign focus its efforts on Product 1 or Product 2?**

# Quick Check ✓

**How many units of each product can be processed through Machine A1 in one minute?**

	<u>Product 1</u>	<u>Product 2</u>
a.	1 unit	0.5 unit
b.	1 unit	2.0 units
c.	2 units	1.0 unit
d.	2 units	0.5 unit

# Quick Check ✓

How many units of each product can be processed through Machine A1 in one minute?

Product 1

Product 2

a. 1 unit

0.5 unit

**b. 1 unit**

**2.0 units**

c. 2 units

1.0 unit

d. 2 units

0.5 unit

## Quick Check ✓

What generates more profit for the company, using one minute of machine A1 to process Product 1 or using one minute of machine A1 to process Product 2?

- a. Product 1
- b. Product 2
- c. They both would generate the same profit.
- d. Cannot be determined.

## Quick Check ✓

What generates more profit for the company, using one minute of machine A1 to process Product 1 or using one minute of machine A1 to process Product 2?

a. Product 1

**b.** Product 2

**With one minute of machine A1, Ensign could make 1 unit of Product 1, with a contribution margin of \$24, or 2 units of Product 2, each with a contribution margin of \$15 per unit.**

$$2 \times \$15 = \$30 > \$24$$

# Utilization of a Constrained Resource

The key is the contribution margin per unit of the constrained resource.

	Product	
	1	2
Contribution margin per unit	\$ 24	\$ 15
Time required to produce one unit	1.00 min.	0.50 min.
Contribution margin per minute	\$ 24	\$ 30

Ensign should emphasize **Product 2** because it generates a contribution margin of \$30 per minute of the constrained resource relative to \$24 per minute for Product 1.

# Utilization of a Constrained Resource

The key is the contribution margin per unit of the constrained resource.

	Product	
	1	2
Contribution margin per unit	\$ 24	\$ 15
Time required to produce one unit	1.00 min.	0.50 min.
Contribution margin per minute	\$ 24	\$ 30

Ensign can maximize its contribution margin by first producing **Product 2** to meet customer demand and then using any remaining capacity to produce Product 1. The calculations would be performed as follows.



# Utilization of a Constrained Resource

**Let's see how this plan would work.**

## **Alloting Our Constrained Resource (Machine A1)**

<b>Weekly demand for Product 2</b>		<b>2,200 units</b>
<b>Time required per unit</b>	<b>×</b>	<b><u>0.50 min.</u></b>
<b>Total time required to make</b>		
<b>Product 2</b>		<b><u><u>1,100 min.</u></u></b>
		<hr/>
		<hr/>
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# Utilization of a Constrained Resource

Let's see how this plan would work.

## Alloting Our Constrained Resource (Machine A1)

Weekly demand for Product 2		2,200	units
Time required per unit	×	<u>0.50</u>	min.
Total time required to make Product 2		<u><u>1,100</u></u>	min.
Total time available		2,400	min.
Time used to make Product 2		<u>1,100</u>	min.
Time available for Product 1		<u><u>1,300</u></u>	min.
		<u>_____</u>	
		<u><u>_____</u></u>	

# Utilization of a Constrained Resource

Let's see how this plan would work.

## Alloting Our Constrained Resource (Machine A1)

Weekly demand for Product 2		2,200	units
Time required per unit	×	<u>0.50</u>	min.
Total time required to make Product 2		<u>1,100</u>	min.
Total time available		2,400	min.
Time used to make Product 2		<u>1,100</u>	min.
Time available for Product 1		1,300	min.
Time required per unit	÷	<u>1.00</u>	min.
Production of Product 1		<u>1,300</u>	units

# Utilization of a Constrained Resource

**According to the plan, we will produce 2,200 units of Product 2 and 1,300 of Product 1. Our contribution margin looks like this.**

	<u>Product 1</u>	<u>Product 2</u>
<b>Production and sales (units)</b>	1,300	2,200
<b>Contribution margin per unit</b>	<u>\$ 24</u>	<u>\$ 15</u>
<b>Total contribution margin</b>	<u><u>\$ 31,200</u></u>	<u><u>\$ 33,000</u></u>

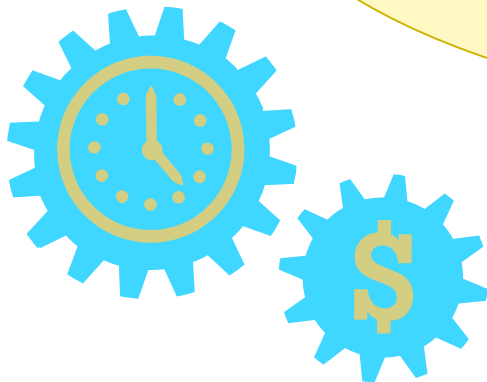
**The total contribution margin for Ensign is \$64,200.**

# Learning Objective

**Determine the value of obtaining more of the constrained resource.**

# Value of a Constrained Resource

**Increasing the capacity of a constrained resource should lead to increased production and sales.**



**How much should Ensign be willing to pay for an additional minute of A1 machine time?**

# Value of a Constrained Resource

**The additional machine time would be used to make more units of Product 1, which had a contribution margin per minute of \$24.**

**Ensign should be willing to pay up to \$24 per minute. This amount equals the contribution margin per minute of machine time that would be earned producing more units of Product 1.**

# Quick Check ✓

**Colonial Heritage makes reproduction colonial furniture from select hardwoods.**

	<i>Chairs</i>	<i>Tables</i>
Selling price per unit	\$80	\$400
Variable cost per unit	\$30	\$200
Board feet per unit	2	10
Monthly demand	600	100

**The company's supplier of hardwood will only be able to supply 2,000 board feet this month. Is this enough hardwood to satisfy demand?**

- a. Yes**
- b. No**



# Quick Check ✓

Colonial Heritage makes reproduction colonial furniture from select hardwoods.

	<i>Chairs</i>	<i>Tables</i>
Selling price per unit	\$80	\$400
Variable cost per unit	\$30	\$200
Board feet per unit	2	10
Monthly demand	600	100

The company's supplier of hardwood will only be able to supply 2,000 board feet this month. Is this enough hardwood to satisfy demand?

a. Yes

**b. No**

$$(2 \times 600) + (10 \times 100) = 2,200 > 2,000$$

# Quick Check ✓

	<i>Chairs</i>	<i>Tables</i>
Selling price per unit	\$80	\$400
Variable cost per unit	\$30	\$200
Board feet per unit	2	10
Monthly demand	600	100

**The company's supplier of hardwood will only be able to supply 2,000 board feet this month. What plan would maximize profits?**

- a. 500 chairs and 100 tables**
- b. 600 chairs and 80 tables**
- c. 500 chairs and 80 tables**
- d. 600 chairs and 100 tables**

# Quick Check ✓

Selling price per  
Variable cost per  
Board feet per  
Monthly demand

*Chairs*     *Tables*

	<i>Chairs</i>	<i>Tables</i>
Selling price	\$ 80	\$ 400
Variable cost	<u>30</u>	<u>200</u>
Contribution margin	\$ 50	\$ 200
Board feet	2	10
CM per board foot	\$ 25	\$ 20
Production of chairs	600	
Board feet required	1,200	
Board feet remaining	800	
Board feet per table	10	
Production of tables		80

The company's supply  
be able to supply 2  
What plan would m

- a. 500 chairs and 1
- b. 600 chairs and 8**
- c. 500 chairs and 8
- d. 600 chairs and 1

## Quick Check ✓

**As before, Colonial Heritage's supplier of hardwood will only be able to supply 2,000 board feet this month. Assume the company follows the plan we have proposed. Up to how much should Colonial Heritage be willing to pay above the usual price to obtain more hardwood?**

- a. \$40 per board foot**
- b. \$25 per board foot**
- c. \$20 per board foot**
- d. Zero**

## Quick Check ✓

The additional wood would be used to make tables. In this use, each board foot of additional wood will allow the company to earn an additional \$20 of contribution margin and profit.

a. \$40 per board foot

b. \$25 per board foot

**c. \$20 per board foot**

d. Zero

# Managing Constraints

**It is often possible for a manager to increase the capacity of a bottleneck, which is called relaxing (or elevating) the constraint, in numerous ways such as:**

- 1. Working overtime on the bottleneck.**
- 2. Subcontracting some of the processing that would be done at the bottleneck.**
- 3. Investing in additional machines at the bottleneck.**
- 4. Shifting workers from non-bottleneck processes to the bottleneck.**
- 5. Focusing business process improvement efforts on the bottleneck.**
- 6. Reducing defective units processed through the bottleneck.**

# Learning Objective

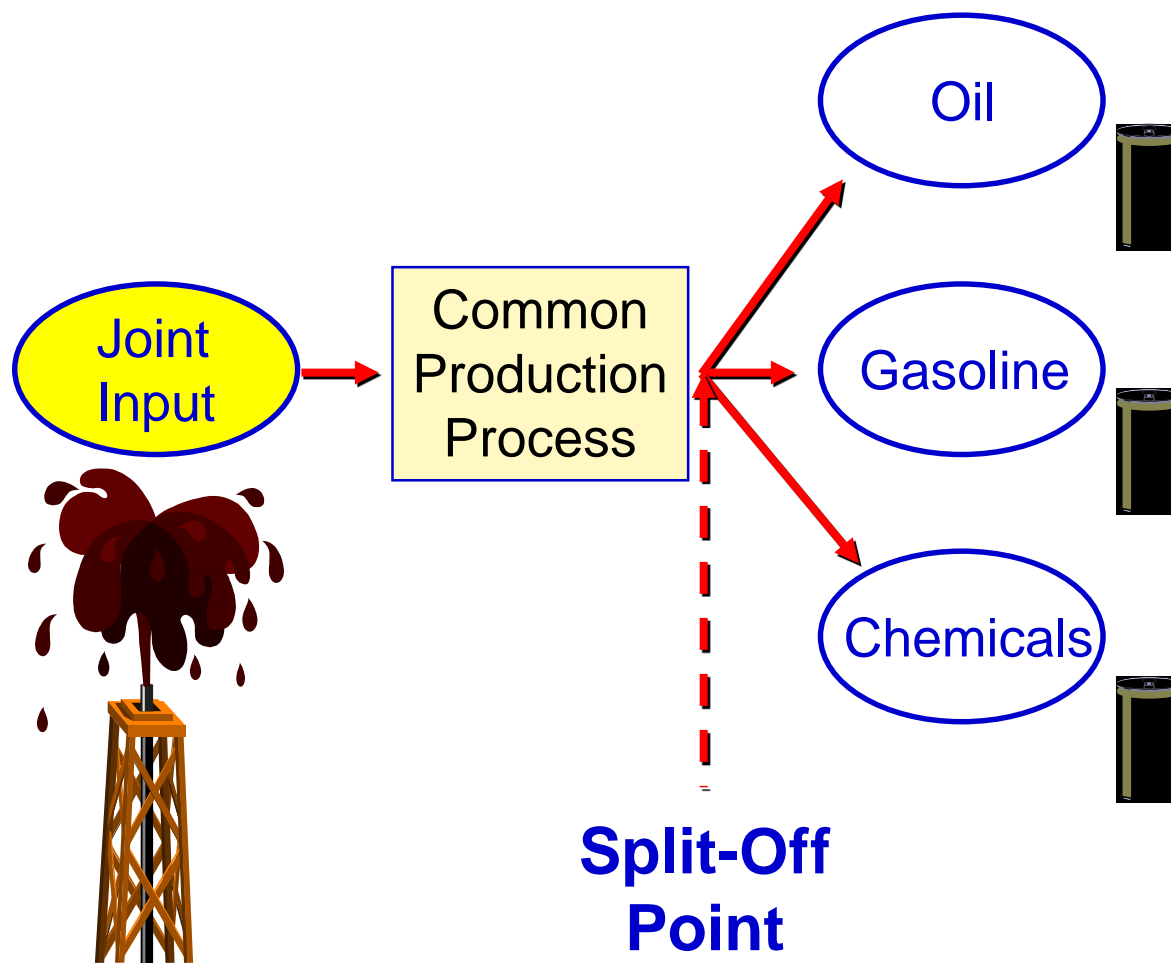
**Prepare an analysis showing whether joint products should be sold at the split-off point or processed further.**

# Joint Costs

- In some industries, a number of end products are produced from a single raw material input.
- Two or more products produced from a common input are called **joint products**.
- The point in the manufacturing process where each joint product can be recognized as a separate product is called the **split-off point**.

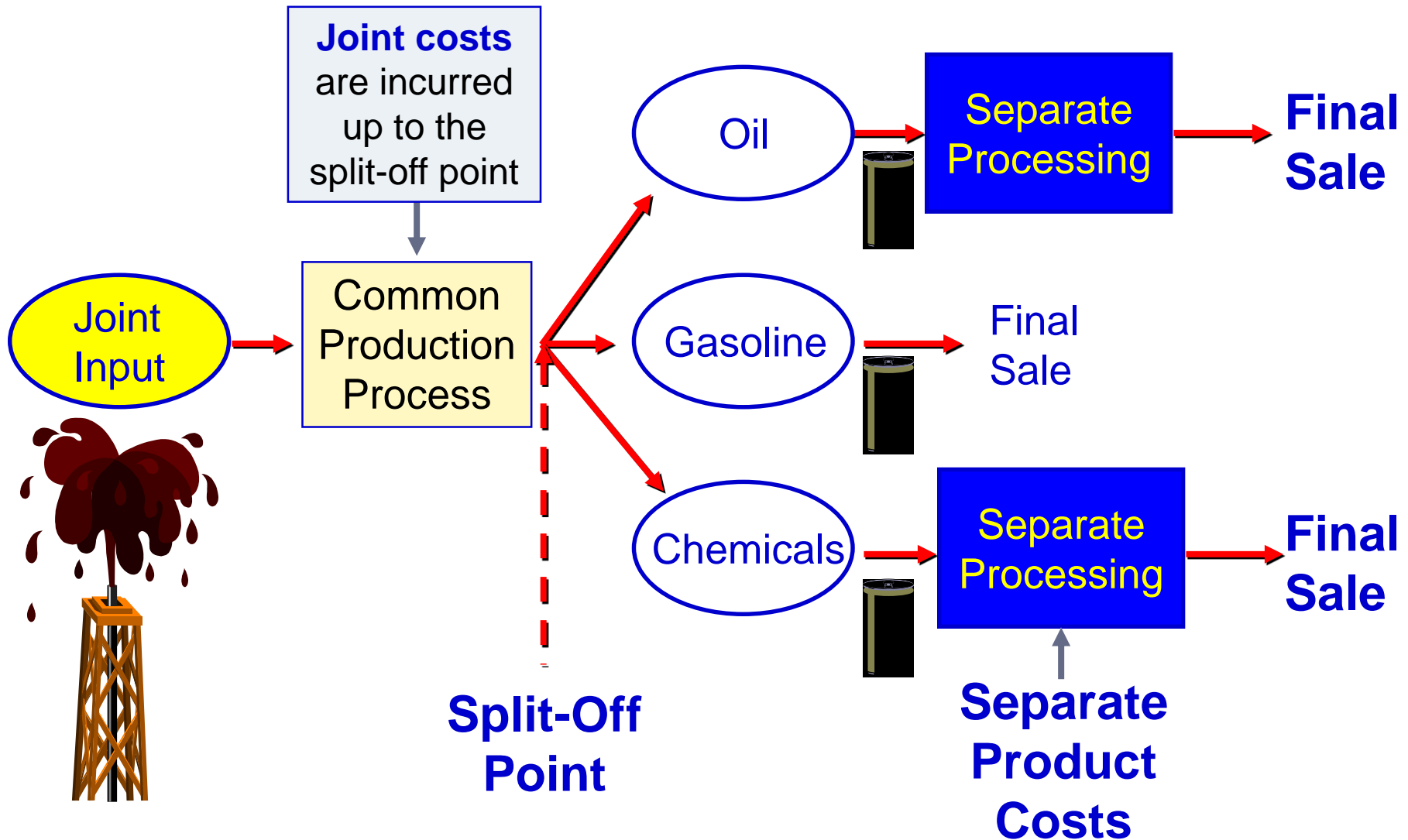


# Joint Products



For example, in the petroleum refining industry, a large number of products are extracted from crude oil, including gasoline, jet fuel, home heating oil, lubricants, asphalt, and various organic chemicals.

# Joint Products



# The Pitfalls of Allocation



Joint costs are traditionally allocated among different products at the split-off point. A typical approach is to allocate joint costs according to the **relative sales value** of the end products.

Although allocation is needed for some purposes such as balance sheet inventory valuation, allocations of this kind are **very dangerous** for decision making.

# Sell or Process Further

**Joint costs are irrelevant in decisions regarding what to do with a product from the split-off point forward. Therefore, these costs should not be allocated to end products for decision-making purposes.**

**With respect to sell or process further decisions, it is profitable to continue processing a joint product after the split-off point **so long as the incremental revenue from such processing exceeds the incremental processing costs incurred after the split-off point.****

# Sell or Process Further: An Example

- Sawmill, Inc. cuts logs from which unfinished lumber and sawdust are the immediate joint products.
- Unfinished lumber is sold “as is” or processed further into finished lumber.
- Sawdust can also be sold “as is” to gardening wholesalers or processed further into “presto-logs.”



# Sell or Process Further

Data about Sawmill's joint products includes:

	<b>Per Log</b>	
	<u>Lumber</u>	<u>Sawdust</u>
<b>Sales value at the split-off point</b>	<b>\$ 140</b>	<b>\$ 40</b>
<b>Sales value after further processing</b>	<b>270</b>	<b>50</b>
<b>Allocated joint product costs</b>	<b>176</b>	<b>24</b>
<b>Cost of further processing</b>	<b>50</b>	<b>20</b>



# Sell or Process Further

## Analysis of Sell or Process Further

	Per Log	
	Lumber	Sawdust
Sales value after further processing	\$ 270	\$ 50
Sales value at the split-off point	140	40
<b>Incremental revenue</b>	<b>130</b>	<b>10</b>
Cost of further processing		
Profit (loss) from further processing		



# Sell or Process Further

## Analysis of Sell or Process Further

	Per Log	
	Lumber	Sawdust
Sales value after further processing	\$ 270	\$ 50
Sales value at the split-off point	140	40
<b>Incremental revenue</b>	<b>130</b>	<b>10</b>
Cost of further processing	50	20
<b>Profit (loss) from further processing</b>	<b>\$ 80</b>	<b>\$ (10)</b>





# Sell or Process Further

## Analysis of Sell or Process Further

	Per Log	
	Lumber	Sawdust
Sales value after further processing	\$ 270	\$ 50
Sales value at the split-off point	140	40
<b>Incremental revenue</b>	<b>130</b>	<b>10</b>
Cost of further processing	50	20
<b>Profit (loss) from further processing</b>	<b>\$ 80</b>	<b>\$ (10)</b>

The lumber should be processed further and the sawdust should be sold at the split-off point.

